

(DN) Copy and complete the statement:

In lesson 4.1, SAS stood for \_\_\_\_\_. In this lesson, ASA will stand for \_\_\_\_\_ and SSS will stand for \_\_\_\_\_.

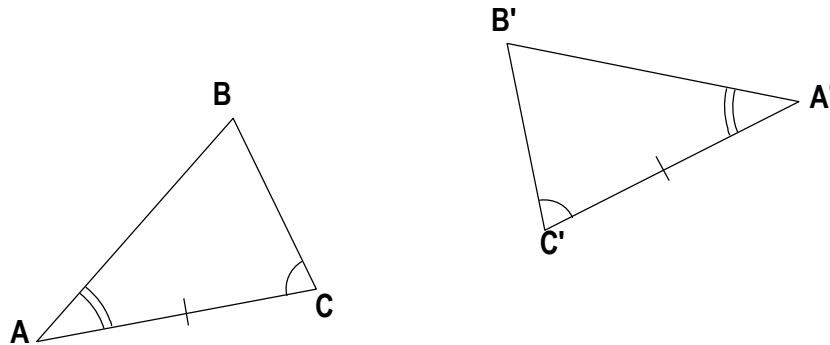
Name \_\_\_\_\_ Per \_\_\_\_\_

LO: I can determine whether or not two triangles can be proven congruent by  $ASA \cong$  or  $SSS \cong$  and use the shortcut to prove that triangles or their parts are congruent.

(1) **Congruence: A sequence of transformations**

transparencies, dry erase markers, eraser, compass, straightedge

Two shapes are congruent if there is a sequence of transformations (1 or more) that map one shape to the other. Determine a sequence of transformations that maps  $\triangle A'B'C'$  back to  $\triangle ABC$ . Write a description and justification for each step in the sequence of transformations.

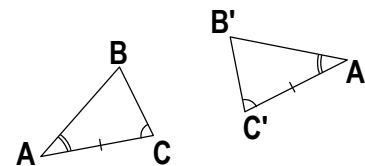


(1b) **Congruence: A sequence of transformations (remix)**

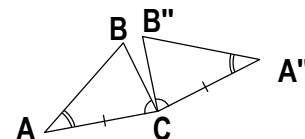
cont.

Prove: If, in a triangle, we know that two pairs of corresponding angles and the pair of corresponding sides between them are congruent, then two triangles are congruent.

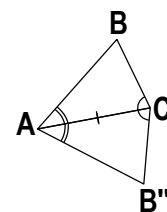
① I am given \_\_\_\_\_  
with \_\_\_\_\_  $\cong$  \_\_\_\_\_, \_\_\_\_\_  $\cong$  \_\_\_\_\_, and \_\_\_\_\_  $\cong$  \_\_\_\_\_.  
(Describe the shapes and the parts that are marked congruent.)



② I \_\_\_\_\_  $\triangle$  \_\_\_\_\_ along vector \_\_\_\_\_ so that \_\_\_\_\_ coincides with \_\_\_\_\_.  
(How did ABC transform?)



③ I \_\_\_\_\_  $\triangle$  \_\_\_\_\_ around \_\_\_\_\_ so that \_\_\_\_\_ coincides with \_\_\_\_\_. I know that \_\_\_\_\_ and \_\_\_\_\_ coincide because \_\_\_\_\_ preserves \_\_\_\_\_ and \_\_\_\_\_  $\cong$  \_\_\_\_\_,  
(How did A'B'C' transform?)

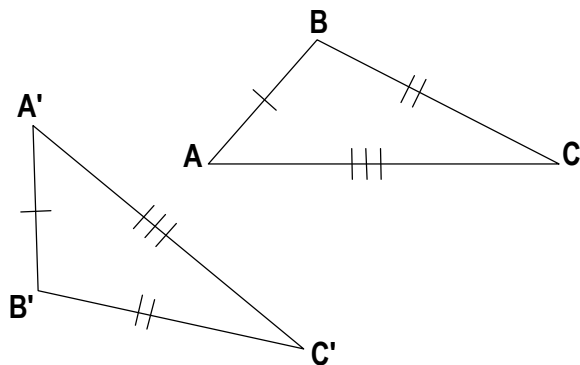


④ I \_\_\_\_\_  $\triangle$  \_\_\_\_\_ across \_\_\_\_\_ so that \_\_\_\_\_ coincides with \_\_\_\_\_. I know that \_\_\_\_\_ and \_\_\_\_\_ coincide because (1)  $\angle$  \_\_\_\_\_  $\cong$   $\angle$  \_\_\_\_\_ which means ray \_\_\_\_\_ coincides with ray \_\_\_\_\_, (2)  $\angle$  \_\_\_\_\_  $\cong$   $\angle$  \_\_\_\_\_ which means ray \_\_\_\_\_ coincides with ray \_\_\_\_\_. Point \_\_\_\_\_ must coincide with \_\_\_\_\_ because 2 noncollinear rays can intersect in, at most, \_\_\_\_\_ point which means \_\_\_\_\_ and \_\_\_\_\_ must \_\_\_\_\_ when reflected across line segment AC.  
(How did A'B''C'' transform?)

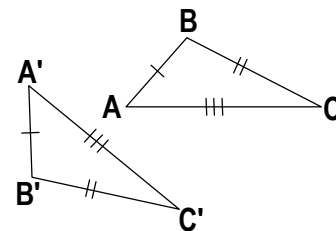
⑤ If we know that \_\_\_\_\_  
then \_\_\_\_\_  
Therefore A \_\_\_\_\_ S \_\_\_\_\_ A \_\_\_\_\_ is a shortcut for proving triangles congruent.  
The pair of \_\_\_\_\_ must be \_\_\_\_\_ the pair of \_\_\_\_\_.  
(What were we trying to prove? Did we prove it?)

(2)  **Congruence: A sequence of transformations**

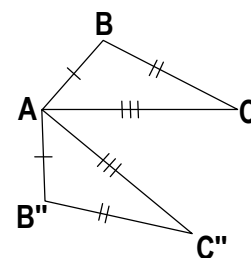
Two shapes are congruent if there is a sequence of transformations (1 or more) that map one shape to the other. Determine a sequence of transformations that maps  $\triangle A'B'C'$  back to  $\triangle ABC$ . Write a description and justification for each step in the sequence of transformations.



(2b)  Prove: If three pairs of corresponding sides are congruent for two triangles, then two triangles are congruent.

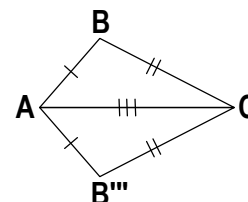


① I am given \_\_\_\_\_  
 with \_\_\_\_\_  $\cong$  \_\_\_\_\_, \_\_\_\_\_  $\cong$  \_\_\_\_\_, and \_\_\_\_\_  $\cong$  \_\_\_\_\_.  
 (Describe the shapes and the parts that are marked congruent.)



② I \_\_\_\_\_  $\triangle$  \_\_\_\_\_ along vector \_\_\_\_\_ so that \_\_\_\_\_ coincides with \_\_\_\_\_.  
 (How did ABC transform?)

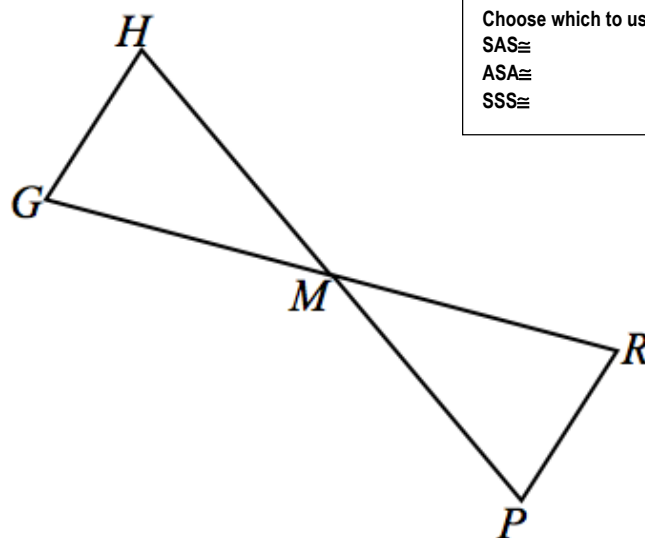
③ I \_\_\_\_\_  $\triangle$  \_\_\_\_\_ around \_\_\_\_\_ so that \_\_\_\_\_ coincides with \_\_\_\_\_. I know that \_\_\_\_\_ and \_\_\_\_\_ coincide because \_\_\_\_\_ preserves \_\_\_\_\_ and \_\_\_\_\_  $\cong$  \_\_\_\_\_,  
 (How did A''B''C'' transform?)



④ I \_\_\_\_\_  $\triangle$  \_\_\_\_\_ across \_\_\_\_\_ so that \_\_\_\_\_ coincides with \_\_\_\_\_. I know that \_\_\_\_\_ and \_\_\_\_\_ coincide because \_\_\_\_\_  $\cong$  \_\_\_\_\_ and \_\_\_\_\_  $\cong$  \_\_\_\_\_. Point \_\_\_\_\_ must coincide with \_\_\_\_\_ because, by construction, the greatest number of points that are given distances from each of two endpoints of a segment is \_\_\_\_\_, and these points are \_\_\_\_\_ of one another. This means \_\_\_\_\_ and \_\_\_\_\_ must \_\_\_\_\_ when reflected across line segment AC.  
 (How did A''B''C'' transform?)

⑤ If we know that \_\_\_\_\_  
 then \_\_\_\_\_  
 Therefore S \_\_\_\_\_ S \_\_\_\_\_ S \_\_\_\_\_ is a shortcut for proving triangles congruent.  
 (What were we trying to prove? Did we prove it?)

- (3)  Given:  $M$  is the midpoint of  $\overline{HP}$ ,  $\angle H \cong \angle P$   
Prove: Two triangle are congruent



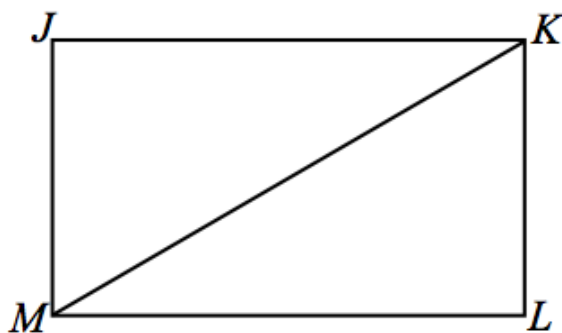
Choose which to use  
SAS $\cong$   
ASA $\cong$   
SSS $\cong$

I know that . . .	because . . .

(4)  Given: JKLM is a rectangle with diagonal KM

Prove: Two triangles are congruent

Choose which to use  
SAS $\cong$   
ASA $\cong$   
SSS $\cong$



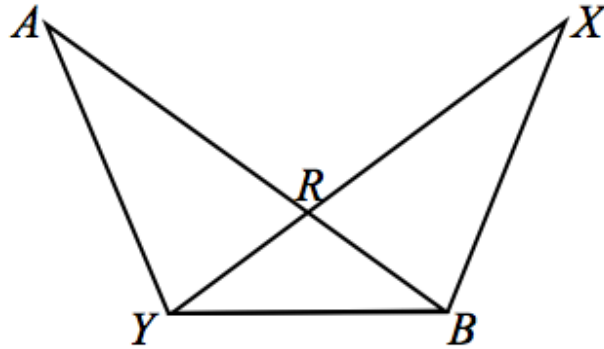
I know that . . .

because . . .


□ (11) □ Given:  $\overline{RY} \cong \overline{RB}$ ,  $\overline{AR} \cong \overline{XR}$

Prove:  $\triangle ARY \cong$  to another triangle

Choose which to use  
 SAS $\cong$   
 ASA $\cong$   
 SSS $\cong$

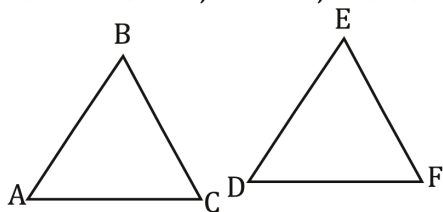


I know that ...

because ...


□ (12) **Exit Ticket**

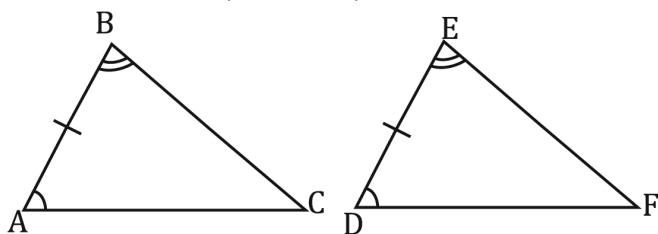
□ Given:  $\overline{BC} \cong \overline{EF}$ ,  $\angle B \cong \angle E$ , and  $\angle C \cong \angle F$



Prove:  $\triangle ABC \cong \triangle DEF$

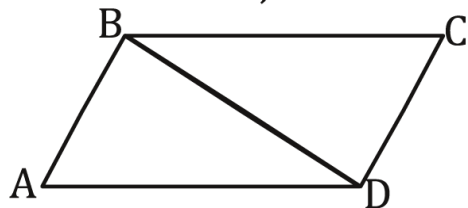
□ (13) **Homework**

(1) Given:  $\overline{AB} \cong \overline{DE}$ ,  $\angle B \cong \angle E$ , and  $\angle A \cong \angle D$



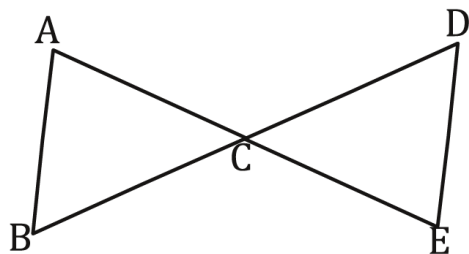
Prove:  $\triangle ABC \cong \triangle DEF$

(2) Given:  $\overline{AB} \cong \overline{CD}$ ,  $\overline{AD} \cong \overline{CB}$



Prove:  $\triangle ABD \cong \triangle CBD$

(3) Given:  $\overline{AE}$  Bisects  $\overline{BD}$ ,  $\angle B \cong \angle D$



Prove:  $\triangle ABC \cong \triangle DBC$